

Package ‘gips’

August 2, 2025

Type Package

Title Gaussian Model Invariant by Permutation Symmetry

Version 1.2.3

Description Find the permutation symmetry group such that the covariance matrix of the given data is approximately invariant under it. Discovering such a permutation decreases the number of observations needed to fit a Gaussian model, which is of great use when it is smaller than the number of variables. Even if that is not the case, the covariance matrix found with 'gips' approximates the actual covariance with less statistical error. The methods implemented in this package are described in Graczyk et al. (2022) <[doi:10.1214/22-AOS2174](https://doi.org/10.1214/22-AOS2174)>. Documentation about 'gips' is provided via its website at <<https://przechoj.github.io/gips/>> and the paper by Chojecki, Morgen, Kołodziejek (2025, <[doi:10.18637/jss.v112.i07](https://doi.org/10.18637/jss.v112.i07)>).

License GPL (>= 3)

URL <https://github.com/PrzeChoj/gips>, <https://przechoj.github.io/gips/>

BugReports <https://github.com/PrzeChoj/gips/issues>

Depends R (>= 3.5.0)

Imports numbers, permutations, rlang (>= 0.4.10), utils

Suggests DAAG, dplyr, ggplot2, graphics, hash, HSAUR2, knitr, MASS (>= 7.3-39), mvtnorm, rmarkdown, spelling, stringi, testthat (>= 3.0.0), tibble, tidyr, withr

VignetteBuilder knitr

Config/testthat/edition 3

Encoding UTF-8

Language en-US

RoxygenNote 7.3.2

NeedsCompilation no

Author Adam Przemysław Chojecki [aut, cre],
Paweł Morgen [aut],
Bartosz Kołodziejek [aut] (ORCID:
<<https://orcid.org/0000-0002-5220-9012>>)
Maintainer Adam Przemysław Chojecki <adam.prze.choj@gmail.com>
Repository CRAN
Date/Publication 2025-03-18 08:30:10 UTC

Contents

AIC.gips	2
as.character.gips	4
as.character.gips_perm	4
calculate_gamma_function	5
compare_posteriories_of_perms	6
find_MAP	8
forget_perms	11
get_probabilities_from_gips	12
get_structure_constants	13
gips	14
gips_perm	17
logLik.gips	19
log_posteriori_of_gips	20
plot.gips	22
prepare_orthogonal_matrix	24
print.gips	26
print.gips_perm	27
project_matrix	27
summary.gips	29
Index	33

AIC.gips	<i>Akaike’s An Information Criterion for gips class</i>
----------	---

Description

Akaike’s An Information Criterion for gips class

Usage

```
## S3 method for class 'gips'  
AIC(object, ..., k = 2)  
  
## S3 method for class 'gips'  
BIC(object, ...)
```

Arguments

object	An object of class gips. Usually, a result of a <code>find_MAP()</code> .
...	Further arguments will be ignored.
k	Numeric, the <i>penalty</i> per parameter to be used. The default k = 2 is the classical AIC.

Value

AIC.gips() returns calculated Akaike's An Information Criterion

When the multivariate normal model does not exist (`number_of_observations < n0`), it returns NULL. When the multivariate normal model cannot be reasonably approximated (output of `project_matrix()` is singular), it returns Inf.

In both failure situations, shows a warning. More information can be found in the **Existence of likelihood** section of `logLik.gips()`.

BIC.gips() returns calculated Schwarz's Bayesian Information Criterion.

Functions

- BIC(gips): Schwarz's Bayesian Information Criterion

Calculation details

For more details and used formulas, see the **Information Criterion - AIC and BIC** section in `vignette("Theory", package = "gips")` or its [pkgdown page](#).

See Also

- `AIC()`, `BIC()` - Generic functions this AIC.gips() and BIC.gips() extend.
- `find_MAP()` - Usually, the AIC.gips() and BIC.gips() are called on the output of `find_MAP()`.
- `logLik.gips()` - Calculates the log-likelihood for the gips object. An important part of the Information Criteria.

Examples

```
S <- matrix(c(
  5.15, 2.05, 3.10, 1.99,
  2.05, 5.09, 2.03, 3.07,
  3.10, 2.03, 5.21, 1.97,
  1.99, 3.07, 1.97, 5.13
), nrow = 4)
g <- gips(S, 14)
g_map <- find_MAP(g, optimizer = "brute_force")

AIC(g) # 238
AIC(g_map) # 224 < 238, so g_map is better than g according to AIC
# =====
BIC(g) # 244
BIC(g_map) # 226 < 244, so g_map is better than g according to BIC
```

as.character.gips	<i>Transform the gips object to a character vector</i>
-------------------	--

Description

Implementation of the S3 method.

Usage

```
## S3 method for class 'gips'
as.character(x, ...)
```

Arguments

x	An object of a gips class.
...	Further arguments (currently ignored).

Value

Returns an object of a character type.

See Also

- [as.character.gips_perm\(\)](#) - The underlying gips_perm of the gips object is passed to [as.character.gips_perm\(\)](#).
- [permutations::as.character.cycle\(\)](#) - The underlying permutation of the gips object is passed to [permutations::as.character.cycle\(\)](#).

Examples

```
A <- matrix(rnorm(4 * 4), nrow = 4)
S <- t(A) %*% A
g <- gips(S, 14, perm = "(123)")
as.character(g)
```

as.character.gips_perm	<i>Transform the gips_perm object to a character vector</i>
------------------------	---

Description

Implementation of the S3 method.

Usage

```
## S3 method for class 'gips_perm'
as.character(x, ...)
```

Arguments

`x` An object of a `gips_perm` class.

`...` Further arguments (currently ignored).

Value

Returns an object of a character type.

See Also

- `as.character.gips()` - The underlying `gips_perm` of the `gips` object is passed to `as.character.gips_perm()`.
- `permutations::as.character.cycle()` - The underlying permutation of the `gips` object is passed to `permutations::as.character.cycle()`.

Examples

```
g_perm <- gips_perm("(5,4)", 5)
as.character(g_perm)
```

calculate_gamma_function

Calculate Gamma function

Description

It calculates the value of the integral defined in [Definition 11 from references](#). It implements [Theorem 8 from references](#) and uses the [formula \(19\) from references](#).

Usage

```
calculate_gamma_function(perm, lambda)
```

Arguments

`perm` An object of a `gips_perm` class. It can also be of a `gips` class, but it will be interpreted as the underlying `gips_perm`.

`lambda` A positive real number.

Value

Returns the value of the Gamma function of the colored cone (for the definition of the colored cone, see the **Basic definitions** section in `vignette("Theory", package = "gips")` or in its [pkgdown page](#)).

References

Piotr Graczyk, Hideyuki Ishi, Bartosz Kołodziejek, Hélène Massam. "Model selection in the space of Gaussian models invariant by symmetry." The Annals of Statistics, 50(3) 1747-1774 June 2022.
[arXiv link](#); [doi:10.1214/22AOS2174](#)

See Also

- `get_structure_constants()` - The function useful inside the `calculate_gamma_function()`.
- `log_posteriori_of_gips()` - The function that uses the values of the gamma function.
- `vignette("Theory", package = "gips")` or its [pkgdown page](#) - A place to learn more about the math behind the gips package.

Examples

```
id_perm <- gips_perm("()", 2)
calculate_gamma_function(id_perm, 0.5001) # 10.7...
calculate_gamma_function(id_perm, 0.50000001) # 19.9...
calculate_gamma_function(id_perm, 0.500000000001) # 29.1...

oldw <- getOption("warn")
options(warn = -1)
calculate_gamma_function(id_perm, 0.5) # Inf
# Integral diverges; returns Inf and warning
options(warn = oldw)
```

compare_posteriories_of_perms

Compare the posteriori probabilities of 2 permutations

Description

Check which permutation is more likely and how much more likely.

Usage

```
compare_posteriories_of_perms(
  perm1,
  perm2 = "()",
  S = NULL,
  number_of_observations = NULL,
  delta = 3,
  D_matrix = NULL,
  was_mean_estimated = TRUE,
  print_output = TRUE,
  digits = 3
)
```

```

compare_log_posteriories_of_perms(
  perm1,
  perm2 = "()",
  S = NULL,
  number_of_observations = NULL,
  delta = 3,
  D_matrix = NULL,
  was_mean_estimated = TRUE,
  print_output = TRUE,
  digits = 3
)

```

Arguments

perm1, perm2	Permutations to compare. How many times perm1 is more likely than perm2? Those can be provided as the gips objects, the gips_perm objects, or anything that can be used as the x parameter in the gips_perm() function. They do not have to be of the same class.
S, number_of_observations, delta, D_matrix, was_mean_estimated	The same parameters as in the gips() function. If at least one of perm1 or perm2 is a gips object, they are overwritten with those from the gips object.
print_output	A boolean. When TRUE (default), the computed value will be printed with additional text and returned invisibly. When FALSE, the computed value will be returned visibly.
digits	Integer. Only used when print_output = TRUE. The number of digits after the comma to print. It can be negative, can be +Inf. It is passed to <code>base::round()</code> .

Value

The function `compare_posteriories_of_perms()` returns the value of how many times the perm1 is more likely than perm2.

The function `compare_log_posteriories_of_perms()` returns the logarithm of how many times the perm1 is more likely than perm2.

Functions

- `compare_log_posteriories_of_perms()`: More stable, logarithmic version of `compare_posteriories_of_perms()`. The natural logarithm is used.

See Also

- [print.gips\(\)](#) - The function that prints the posterior of the optimized gips object compared to the starting permutation.
- [summary.gips\(\)](#) - The function that calculates the posterior of the optimized gips object compared to the starting permutation.
- [find_MAP\(\)](#) - The function that finds the permutation that maximizes `log_posteriori_of_gips()`.
- [log_posteriori_of_gips\(\)](#) - The function this `compare_posteriories_of_perms()` calls underneath.

Examples

```
require("MASS") # for mvrnorm()

perm_size <- 6
mu <- runif(6, -10, 10) # Assume we don't know the mean
sigma_matrix <- matrix(
  data = c(
    1.05, 0.8, 0.6, 0.4, 0.6, 0.8,
    0.8, 1.05, 0.8, 0.6, 0.4, 0.6,
    0.6, 0.8, 1.05, 0.8, 0.6, 0.4,
    0.4, 0.6, 0.8, 1.05, 0.8, 0.6,
    0.6, 0.4, 0.6, 0.8, 1.05, 0.8,
    0.8, 0.6, 0.4, 0.6, 0.8, 1.05
  ),
  nrow = perm_size, byrow = TRUE
) # sigma_matrix is a matrix invariant under permutation (1,2,3,4,5,6)
number_of_observations <- 13
Z <- MASS::mvrnorm(number_of_observations, mu = mu, Sigma = sigma_matrix)
S <- cov(Z) # Assume we have to estimate the mean

g <- gips(S, number_of_observations)
g_map <- find_MAP(g, max_iter = 10, show_progress_bar = FALSE, optimizer = "Metropolis-Hastings")

compare_posteriories_of_perms(g_map, g, print_output = TRUE)
exp(compare_log_posteriories_of_perms(g_map, g, print_output = FALSE))
```

find_MAP

Find the Maximum A Posteriori Estimation

Description

Use one of the optimization algorithms to find the permutation that maximizes a posteriori probability based on observed data. Not all optimization algorithms will always find the MAP, but they try to find a significant value. More information can be found in the "**Possible algorithms to use as optimizers**" section below.

Usage

```
find_MAP(
  g,
  max_iter = NA,
  optimizer = NA,
  show_progress_bar = TRUE,
  save_all_perms = FALSE,
  return_probabilities = FALSE
)
```


Arguments

<code>g</code>	Object of a gips class.
<code>max_iter</code>	The number of iterations for an algorithm to perform. At least 2. For optimizer = "BF", it is not used; for optimizer = "MH", it has to be finite; for optimizer = "HC", it can be infinite.
<code>optimizer</code>	The optimizer for the search of the maximum posteriori: • "BF" (the default for unoptimized g with perm size <= 9) - Brute Force; • "MH" (the default for unoptimized g with perm size > 10) - Metropolis-Hastings; • "HC" - Hill Climbing; • "continue" (the default for optimized g) - The same as the g was optimized by (see Examples). See the Possible algorithms to use as optimizers section below for more details.
<code>show_progress_bar</code>	A boolean. Indicate whether or not to show the progress bar: • When max_iter is infinite, show_progress_bar has to be FALSE; • When return_probabilities = TRUE, then shows an additional progress bar for the time when the probabilities are calculated.
<code>save_all_perms</code>	A boolean. TRUE indicates saving a list of all permutations visited during optimization. This can be useful sometimes but needs a lot more RAM.
<code>return_probabilities</code>	A boolean. TRUE can only be provided only when save_all_perms = TRUE. For: • optimizer = "MH" - use Metropolis-Hastings results to estimate posterior probabilities; • optimizer = "BF" - use brute force results to calculate exact posterior probabilities. These additional calculations are costly, so a second and third progress bar is shown (when show_progress_bar = TRUE). To examine probabilities after optimization, call get_probabilities_from_gips().

Details

find_MAP() can produce a warning when:

- the optimizer "hill_climbing" gets to the end of its max_iter without converging.
- the optimizer will find the permutation with smaller n_0 than number_of_observations (for more information on what it means, see C_σ **and** n_0 section in the vignette("Theory", package = "gips") or in its [pkgdown page](#)).

Value

Returns an optimized object of a gips class.

Possible algorithms to use as optimizers

For an in-depth explanation, see in the vignette("Optimizers", package = "gips") or in its [pkgdown page](#).

For every algorithm, there are some aliases available.

- "brute_force", "BF", "full" - use the **Brute Force** algorithm that checks the whole permutation space of a given size. This algorithm will find the actual Maximum A Posteriori Estimation, but it is very computationally expensive for bigger spaces. We recommend Brute Force only for $p \leq 9$. For the time the Brute Force takes on our machines, see in the vignette("Optimizers", package = "gips") or in its [pkgdown page](#).
- "Metropolis_Hastings", "MH" - use the **Metropolis-Hastings** algorithm; [see Wikipedia](#). The algorithm will draw a random transposition in every iteration and consider changing the current state (permutation). When the max_iter is reached, the algorithm will return the best permutation calculated as the MAP Estimator. This implements the [Second approach from references, section 4.1.2](#). This algorithm used in this context is a special case of the **Simulated Annealing** the user may be more familiar with; [see Wikipedia](#).
- "hill_climbing", "HC" - use the **hill climbing** algorithm; [see Wikipedia](#). The algorithm will check all transpositions in every iteration and go to the one with the biggest a posteriori value. The optimization ends when all *neighbors* will have a smaller a posteriori value. If the max_iter is reached before the end, then the warning is shown, and it is recommended to continue the optimization on the output of the find_MAP() with optimizer = "continue"; see examples. Remember that $p*(p-1)/2$ transpositions will be checked in every iteration. For bigger p, this may be costly.

References

Piotr Graczyk, Hideyuki Ishi, Bartosz Kołodziejek, H  l  ne Massam. "Model selection in the space of Gaussian models invariant by symmetry." The Annals of Statistics, 50(3) 1747-1774 June 2022. [arXiv link](#); doi:10.1214/22AOS2174

See Also

- [gips\(\)](#) - The constructor of a gips class. The gips object is used as the g parameter of find_MAP().
- [plot.gips\(\)](#) - Practical plotting function for visualizing the optimization process.
- [summary.gips\(\)](#) - Summarize the output of optimization.
- [AIC.gips\(\)](#), [BIC.gips\(\)](#) - Get the Information Criterion of the found model.
- [get_probabilities_from_gips\(\)](#) - When find_MAP(return_probabilities = TRUE) was called, probabilities can be extracted with this function.
- [log_posteriori_of_gips\(\)](#) - The function that the optimizers of find_MAP() tries to find the argmax of.
- [forget_perms\(\)](#) - When the gips object was optimized with find_MAP(save_all_perms = TRUE), it will be of considerable size in RAM. forget_perms() can make such an object lighter in memory by forgetting the permutations it visited.
- vignette("Optimizers", package = "gips") or its [pkgdown page](#) - A place to learn more about the available optimizers.

- `vignette("Theory", package = "gips")` or its [pkgdown page](#) - A place to learn more about the math behind the gips package.

Examples

```
require("MASS") # for mvrnorm()

perm_size <- 5
mu <- runif(perm_size, -10, 10) # Assume we don't know the mean
sigma_matrix <- matrix(
  data = c(
    1.0, 0.8, 0.6, 0.6, 0.8,
    0.8, 1.0, 0.8, 0.6, 0.6,
    0.6, 0.8, 1.0, 0.8, 0.6,
    0.6, 0.6, 0.8, 1.0, 0.8,
    0.8, 0.6, 0.6, 0.8, 1.0
  ),
  nrow = perm_size, byrow = TRUE
) # sigma_matrix is a matrix invariant under permutation (1,2,3,4,5)
number_of_observations <- 13
Z <- MASS::mvrnorm(number_of_observations, mu = mu, Sigma = sigma_matrix)
S <- cov(Z) # Assume we have to estimate the mean

g <- gips(S, number_of_observations)

g_map <- find_MAP(g, max_iter = 5, show_progress_bar = FALSE, optimizer = "Metropolis_Hastings")
g_map

g_map2 <- find_MAP(g_map, max_iter = 5, show_progress_bar = FALSE, optimizer = "continue")

if (require("graphics")) {
  plot(g_map2, type = "both", logarithmic_x = TRUE)
}

g_map_BF <- find_MAP(g, show_progress_bar = FALSE, optimizer = "brute_force")
summary(g_map_BF)
```

forget_perms	<i>Forget the permutations for gips object optimized with</i> save_all_perms = TRUE
--------------	--

Description

Slim the gips object by forgetting the visited permutations from `find_MAP(save_all_perms = TRUE)`.

Usage

```
forget_perms(g)
```

Arguments

`g` An object of class `gips`. A result of a `find_MAP(save_all_perms = TRUE)`.

Details

For example, `perm_size = 150` and `max_iter = 150000` we checked `forget_perms()` saves ~350 MB of RAM.

Value

Returns the same object `g` as given, but without the visited permutation list.

See Also

- `find_MAP()` - The `forget_perms()` is called on the output of `find_MAP(save_all_perms = TRUE)`.

Examples

```
A <- matrix(rnorm(10 * 10), nrow = 10)
S <- t(A) %*% A
g <- gips(S, 13, was_mean_estimated = FALSE)
g_map <- find_MAP(g,
  max_iter = 10, optimizer = "Metropolis_Hastings",
  show_progress_bar = FALSE, save_all_perms = TRUE
)

object.size(g_map) # ~18 KB
g_map_slim <- forget_perms(g_map)
object.size(g_map_slim) # ~8 KB
```

```
get_probabilities_from_gips
```

Extract probabilities for gips object optimized with
`return_probabilities = TRUE`

Description

After the `gips` object was optimized with the `find_MAP(return_probabilities = TRUE)` function, then those calculated probabilities can be extracted with this function.

Usage

```
get_probabilities_from_gips(g)
```

Arguments

`g` An object of class `gips`. A result of a `find_MAP(return_probabilities = TRUE)`.

Value

Returns a numeric vector, calculated values of probabilities. Names contain permutations this probabilities represent. For gips object optimized with `find_MAP(return_probabilities = FALSE)`, it returns a NULL object. It is sorted according to the probability.

See Also

- `find_MAP()` - The `get_probabilities_from_gips()` is called on the output of `find_MAP(return_probabilities = TRUE, save_all_perms = TRUE)`.
- `vignette("Optimizers", package = "gips")` or its [pkgdown page](#) - A place to learn more about the available optimizers.

Examples

```
g <- gips(matrix(c(1, 0.5, 0.5, 1.3), nrow = 2), 13, was_mean_estimated = FALSE)
g_map <- find_MAP(g,
  optimizer = "BF", show_progress_bar = FALSE,
  return_probabilities = TRUE, save_all_perms = TRUE
)

get_probabilities_from_gips(g_map)
```

get_structure_constants

Get Structure Constants

Description

Finds constants necessary for internal calculations of integrals and eventually the posteriori probability in `log_posteriori_of_gips()`.

Usage

```
get_structure_constants(perm)
```

Arguments

perm	An object of a gips_perm class. It can also be of a gips class, but it will be interpreted as the underlying gips_perm.
------	---

Details

Uses [Theorem 5 from references](#) to calculate the constants.

Value

Returns a list of 5 items: r, d, k, L, dim_omega - vectors of constants from [Theorem 1 from references](#) and the beginning of [section 3.1. from references](#).

Arguments

<code>S</code>	A matrix; empirical covariance matrix. When <code>Z</code> is the observed data: - if one does not know the theoretical mean and has to estimate it with the observed mean, use <code>S = cov(Z)</code>, and leave parameter <code>was_mean_estimated = TRUE</code> as default; - if one know the theoretical mean is 0, use <code>S = (t(Z) %*% Z) / number_of_observations</code>, and set parameter <code>was_mean_estimated = FALSE</code>.
<code>number_of_observations</code>	A number of data points that <code>S</code> is based on.
<code>delta</code>	A number, hyper-parameter of a Bayesian model. It has to be strictly bigger than 1. See the Hyperparameters section below.
<code>D_matrix</code>	Symmetric, positive-definite matrix of the same size as <code>S</code> . Hyper-parameter of a Bayesian model. When <code>NULL</code> , the (hopefully) reasonable one is derived from the data. For more details, see the Hyperparameters section below.
<code>was_mean_estimated</code>	A boolean. - Set <code>TRUE</code> (default) when your <code>S</code> parameter is a result of a <code>stats::cov()</code> function. - Set <code>FALSE</code> when your <code>S</code> parameter is a result of a <code>(t(Z) %*% Z) / number_of_observations</code> calculation.
<code>perm</code>	An optional permutation to be the base for the <code>gips</code> object. It can be of a <code>gips_perm</code> or a permutation class, or anything the function <code>permutations::permutation()</code> can handle. It can also be of a <code>gips</code> class, but it will be interpreted as the underlying <code>gips_perm</code> .
<code>list_of_gips_perm</code>	A list with a single element of a <code>gips_perm</code> class. The base object for the <code>gips</code> object.
<code>optimization_info</code>	For internal use only. <code>NULL</code> or the list with information about the optimization process.
<code>g</code>	Object to be checked whether it is a proper object of a <code>gips</code> class.

Value

`gips()` returns an object of a `gips` class after the safety checks.

`new_gips()` returns an object of a `gips` class without the safety checks.

`validate_gips()` returns its argument unchanged. If the argument is not a proper element of a `gips` class, it produces an error.

Functions

- `new_gips()`: Constructor. It is only intended for low-level use.
- `validate_gips()`: Validator. It is only intended for low-level use.

Methods for a gips class

- `summary.gips()`
- `plot.gips()`
- `print.gips()`
- `logLik.gips()`
- `AIC.gips()`
- `BIC.gips()`
- `as.character.gips()`

Hyperparameters

We encourage the user to try $D_{\text{matrix}} = d * I$, where I is an identity matrix of a size $p \times p$ and $d > 0$ for some different d . When d is small compared to the data (e.g., $d = 0.1 * \text{mean}(\text{diag}(S))$), bigger structures will be found. When d is big compared to the data (e.g., $d = 100 * \text{mean}(\text{diag}(S))$), the posterior distribution does not depend on the data.

Taking $D_{\text{matrix}} = d * I$ is equivalent to setting $S \leftarrow S / d$.

The default for D_{matrix} is $D_{\text{matrix}} = d * I$, where $d = \text{mean}(\text{diag}(S))$, which is equivalent to modifying S so that the mean value on the diagonal is 1.

In the Bayesian model, the prior distribution for the covariance matrix is a generalized case of [Wishart distribution](#).

For a brief introduction, see the **Bayesian model selection** section in `vignette("Theory", package = "gips")` or in its [pkgdown page](#).

For analysis of the Hyperparameters influence, see **Section 3.2.** of "Learning permutation symmetries with gips in R" by gips developers Adam Chojecki, Paweł Morgen, and Bartosz Kołodziejek, [Journal of Statistical Software](#).

See Also

- `stats::cov()` - The S parameter, as an empirical covariance matrix, is most of the time a result of the `cov()` function. For more information, see [Wikipedia - Estimation of covariance matrices](#).
- `find_MAP()` - The function that finds the Maximum A Posteriori (MAP) Estimator for a given gips object.
- `gips_perm()` - The constructor of a `gips_perm` class. The `gips_perm` object is used as the base object for the gips object. To be more precise, the base object for gips is a one-element list of a `gips_perm` object.

Examples

```
require("MASS") # for mvrnorm()

perm_size <- 5
mu <- runif(5, -10, 10) # Assume we don't know the mean
sigma_matrix <- matrix(
  data = c(
```



```

      1.0, 0.8, 0.6, 0.6, 0.8,
      0.8, 1.0, 0.8, 0.6, 0.6,
      0.6, 0.8, 1.0, 0.8, 0.6,
      0.6, 0.6, 0.8, 1.0, 0.8,
      0.8, 0.6, 0.6, 0.8, 1.0
    ),
    nrow = perm_size, byrow = TRUE
  ) # sigma_matrix is a matrix invariant under permutation (1,2,3,4,5)
  number_of_observations <- 13
  Z <- MASS::mvrnorm(number_of_observations, mu = mu, Sigma = sigma_matrix)
  S <- cov(Z) # Assume we have to estimate the mean

  g <- gips(S, number_of_observations)

  g_map <- find_MAP(g, show_progress_bar = FALSE, optimizer = "brute_force")
  g_map

  summary(g_map)

  if (require("graphics")) {
    plot(g_map, type = "both", logarithmic_x = TRUE)
  }

```

gips_perm*Permutation object*

Description

Create permutation objects to be passed to other functions of the gips package.

Usage

```

gips_perm(x, size)

new_gips_perm(rearranged_cycles, size)

validate_gips_perm(g)

```

Arguments

x	A single object that can be interpreted by the <code>permutations::permutation()</code> function. For example, the character of a form "(1,2)(4,5)". See examples. It can also be of a gips class but it will be interpreted as the underlying gips_perm.
size	An integer. Size of a permutation (AKA cardinality of a set, on which permutation is defined. See examples).
rearranged_cycles	A list of rearranged integer vectors. Each vector corresponds to a single cycle of a permutation.
g	Object to be checked whether it is a proper object of a gips_perm class.

Value

`gips_perm()` returns an object of a `gips_perm` class after the safety checks.

`new_gips_perm()` returns an object of a `gips_perm` class without the safety checks.

`validate_gips_perm()` returns its argument unchanged. If the argument is not a proper element of a `gips_perm` class, it produces an error.

Functions

- `new_gips_perm()`: Constructor. Only intended for low-level use.
- `validate_gips_perm()`: Validator. Only intended for low-level use.

Methods for a gips class

- `as.character.gips_perm()`
- `print.gips_perm()`

See Also

- `project_matrix()` - `gips_perm` is the `perm` parameter of `project_matrix()`.
- `permutations::permutation()` - The constructor for the `x` parameter.
- `gips()` - The constructor for the `gips` class uses the `gips_perm` object as the base object.

Examples

```
# All 7 following lines give the same output:
gperm <- gips_perm("(12)(45)", 5)
gperm <- gips_perm("(1,2)(4,5)", 5)
gperm <- gips_perm(as.matrix(c(2, 1, 3, 5, 4)), 5)
gperm <- gips_perm(t(as.matrix(c(2, 1, 3, 5, 4))), 5) # both way for a matrix works
gperm <- gips_perm(list(list(c(2, 1), c(4, 5))), 5)
gperm <- gips_perm(permutations::as.word(c(2, 1, 3, 5, 4)), 5)
gperm <- gips_perm(permutations::as.cycle("(1,2)(4,5)"), 5)
gperm

# note the necessity of the `size` parameter:
gperm <- gips_perm("(12)(45)", 5)
gperm <- gips_perm("(12)(45)", 7) # this one is a different permutation

try(gperm <- gips_perm("(12)(45)", 4))
# Error, `size` was set to 4, while the permutation has the element 5.
```

logLik.gips

*Extract the Log-Likelihood for gips class***Description**

Calculates Log-Likelihood of the sample based on the gips object.

Usage

```
## S3 method for class 'gips'
logLik(object, ...)
```

Arguments

object An object of class gips. Usually, a result of a `find_MAP()`.
 ... Further arguments will be ignored.

Details

This will always be the biggest for `perm = "()"` (provided that $p \leq n$).

If the found permutation still requires more parameters than n , the likelihood does not exist; thus the function returns NULL.

If the projected_cov (output of `project_matrix()`) is close to singular, the NA is returned.

Value

Log-Likelihood of the sample. Object of class logLik.

Possible failure situations:

- When the multivariate normal model does not exist (`number_of_observations < n0`), it returns NULL.
- When the multivariate normal model cannot be reasonably approximated (output of `project_matrix()` is singular), it returns `-Inf`.

In both failure situations, it shows a warning. More information can be found in the **Existence of likelihood** section below.

Existence of likelihood

We only consider the non-degenerate multivariate normal model. In the gips context, such a model exists only when the number of observations is bigger or equal to $n0$. To get $n0$ for the gips object `g`, call `summary(g)$n0`.

See examples where the `g_n_too_small` had too small `number_of_observations` to have likelihood. After the optimization, the likelihood did exist.

For more information, refer to C_σ **and** $n0$ section in `vignette("Theory", package = "gips")` or its [pkgdown page](#).

Calculation details

For more details and used formulas, see the **Information Criterion - AIC and BIC** section in vignette("Theory", package = "gips") or its [pkgdown page](#).

See Also

- `logLik()` - Generic function this `logLik.gips()` extends.
- `find_MAP()` - Usually, the `logLik.gips()` is called on the output of `find_MAP()`.
- `AIC.gips()`, `BIC.gips()` - Often, one is more interested in an Information Criterion AIC or BIC.
- `summary.gips()` - One can get `n0` by calling `summary(g)$n0`. To see why one may be interested in `n0`, see the **Existence of likelihood** section above.
- `project_matrix()` - Project the known matrix onto the found permutations space. It is mentioned in the **Calculation details** section above.

Examples

```
S <- matrix(c(
  5.15, 2.05, 3.60, 1.99,
  2.05, 5.09, 2.03, 3.57,
  3.60, 2.03, 5.21, 1.97,
  1.99, 3.57, 1.97, 5.13
), nrow = 4)
g <- gips(S, 5)
logLik(g) # -32.67048
# For perm = "()", which is default, there is p + choose(p, 2) degrees of freedom

g_map <- find_MAP(g, optimizer = "brute_force")
logLik(g_map) # -32.6722 # this will always be smaller than `logLik(gips(S, n, perm = ""))`

g_n_too_small <- gips(S, number_of_observations = 4)
logLik(g_n_too_small) # NULL # the likelihood does not exists
summary(g_n_too_small)$n0 # 5, but we set number_of_observations = 4, which is smaller

g_MAP <- find_MAP(g_n_too_small)
logLik(g_MAP) # -24.94048, this is no longer NULL
summary(g_MAP)$n0 # 2
```

log_posteriori_of_gips

A log of a posteriori that the covariance matrix is invariant under permutation

Description

More precisely, it is the logarithm of an unnormalized posterior probability. It is the goal function for optimization algorithms in the `find_MAP()` function. The `perm_proposal` that maximizes this function is the Maximum A Posteriori (MAP) Estimator.

Usage

```
log_posteriori_of_gips(g)
```

Arguments

g An object of a gips class.

Details

It is calculated using [formulas \(33\) and \(27\) from references](#).

If Inf or NaN is reached, it produces a warning.

Value

Returns a value of the logarithm of an unnormalized A Posteriori.

References

Piotr Graczyk, Hideyuki Ishi, Bartosz Kołodziejek, Hélène Massam. "Model selection in the space of Gaussian models invariant by symmetry." The Annals of Statistics, 50(3) 1747-1774 June 2022.
[arXiv link](#); [doi:10.1214/22AOS2174](#)

See Also

- [calculate_gamma_function\(\)](#) - The function that calculates the value needed for `log_posteriori_of_gips()`.
- [get_structure_constants\(\)](#) - The function that calculates the structure constants needed for `log_posteriori_of_gips()`.
- [find_MAP\(\)](#) - The function that optimizes the `log_posteriori_of_gips` function.
- [compare_posteriories_of_perms\(\)](#) - Uses `log_posteriori_of_gips()` to compare a posteriori of two permutations.
- `vignette("Theory", package = "gips")` or its [pkgdown page](#) - A place to learn more about the math behind the gips package.

Examples

```
# In the space with p = 2, there is only 2 permutations:
perm1 <- permutations::as.cycle("(1)(2)")
perm2 <- permutations::as.cycle("(1,2)")
S1 <- matrix(c(1, 0.5, 0.5, 2), nrow = 2, byrow = TRUE)
g1 <- gips(S1, 100, perm = perm1)
g2 <- gips(S1, 100, perm = perm2)
log_posteriori_of_gips(g1) # -134.1615, this is the MAP Estimator
log_posteriori_of_gips(g2) # -138.1695

exp(log_posteriori_of_gips(g1) - log_posteriori_of_gips(g2)) # 55.0
# g1 is 55 times more likely than g2.
# This is the expected outcome because S[1,1] significantly differs from S[2,2].

compare_posteriories_of_perms(g1, g2)
```

```
# The same result, but presented in a more pleasant way

# =====

S2 <- matrix(c(1, 0.5, 0.5, 1.1), nrow = 2, byrow = TRUE)
g1 <- gips(S2, 100, perm = perm1)
g2 <- gips(S2, 100, perm = perm2)
log_posteriori_of_gips(g1) # -98.40984
log_posteriori_of_gips(g2) # -95.92039, this is the MAP Estimator

exp(log_posteriori_of_gips(g2) - log_posteriori_of_gips(g1)) # 12.05
# g2 is 12 times more likely than g1.
# This is the expected outcome because S[1,1] is very close to S[2,2].

compare_posteriories_of_perms(g2, g1)
# The same result, but presented in a more pleasant way
```

plot.gips

Plot optimized matrix or optimization gips object

Description

Plot the heatmap of the MAP covariance matrix estimator or the convergence of the optimization method. The plot depends on the type argument.

Usage

```
## S3 method for class 'gips'
plot(
  x,
  type = NA,
  logarithmic_y = TRUE,
  logarithmic_x = FALSE,
  color = NULL,
  title_text = "Convergence plot",
  xlabel = NULL,
  ylabel = NULL,
  show_legend = TRUE,
  ylim = NULL,
  xlim = NULL,
  ...
)
```

Arguments

x	Object of a gips class.
type	A character vector of length 1. One of c("heatmap", "MLE", "best", "all", "both", "n0", "block_heatmap"):

- "heatmap", "MLE" - Plots a heatmap of the Maximum Likelihood Estimator of the covariance matrix given the permutation. That is, the S matrix inside the gips object projected on the permutation in the gips object.
- "best" - Plots the line of the biggest a posteriori found over time.
- "all" - Plots the line of a posteriori for all visited states.
- "both" - Plots both lines from "all" and "best".
- "n0" - Plots the line of n0s that were spotted during optimization (only for "MH" optimization).
- "block_heatmap" - Plots a heatmap of diagonally block representation of S. Non-block entries (equal to 0) are white for better clarity. For more information, see **Block Decomposition - [1], Theorem 1** section in vignette("Theory", package = "gips") or in its [pkgdown page](#).

The default value is NA, which will be changed to "heatmap" for non-optimized gips objects and to "both" for optimized ones. Using the default produces a warning. All other arguments are ignored for the type = "heatmap", type = "MLE", or type = "block_heatmap".

logarithmic_y, logarithmic_x	A boolean. Sets the axis of the plot in logarithmic scale.
color	Vector of colors to be used to plot lines.
title_text	Text to be in the title of the plot.
xlabel	Text to be on the bottom of the plot.
ylabel	Text to be on the left of the plot.
show_legend	A boolean. Whether or not to show a legend.
ylim	Limits of the y axis. When NULL, the minimum, and maximum of the log_posteriori_of_gips() are taken.
xlim	Limits of the x axis. When NULL, the whole optimization process is shown.
...	Additional arguments passed to other various elements of the plot.

Value

When type is one of "best", "all", "both" or "n0", returns an invisible NULL. When type is one of "heatmap", "MLE" or "block_heatmap", returns an object of class ggplot.

See Also

- [find_MAP\(\)](#) - Usually, the plot.gips() is called on the output of find_MAP().
- [project_matrix\(\)](#) - The function used with type = "MLE".
- [gips\(\)](#) - The constructor of a gips class. The gips object is used as the x parameter.

Examples

```
require("MASS") # for mvrnorm()

perm_size <- 6
mu <- runif(6, -10, 10) # Assume we don't know the mean
```

```

sigma_matrix <- matrix(
  data = c(
    1.0, 0.8, 0.6, 0.4, 0.6, 0.8,
    0.8, 1.0, 0.8, 0.6, 0.4, 0.6,
    0.6, 0.8, 1.0, 0.8, 0.6, 0.4,
    0.4, 0.6, 0.8, 1.0, 0.8, 0.6,
    0.6, 0.4, 0.6, 0.8, 1.0, 0.8,
    0.8, 0.6, 0.4, 0.6, 0.8, 1.0
  ),
  nrow = perm_size, byrow = TRUE
) # sigma_matrix is a matrix invariant under permutation (1,2,3,4,5,6)
number_of_observations <- 13
Z <- MASS::mvrnorm(number_of_observations, mu = mu, Sigma = sigma_matrix)
S <- cov(Z) # Assume we have to estimate the mean

g <- gips(S, number_of_observations)
if (require("graphics")) {
  plot(g, type = "MLE")
}

g_map <- find_MAP(g, max_iter = 30, show_progress_bar = FALSE, optimizer = "hill_climbing")
if (require("graphics")) {
  plot(g_map, type = "both", logarithmic_x = TRUE)
}

if (require("graphics")) {
  plot(g_map, type = "MLE")
}
# Now, the output is (most likely) different because the permutation
# `g_map[[1]]` is (most likely) not an identity permutation.

g_map_MH <- find_MAP(g, max_iter = 30, show_progress_bar = FALSE, optimizer = "MH")
if (require("graphics")) {
  plot(g_map_MH, type = "n0")
}

```

```
prepare_orthogonal_matrix
```

Prepare orthogonal matrix

Description

Calculate the orthogonal matrix U_{Γ} for decomposition in [Theorem 1 from references](#).

Usage

```
prepare_orthogonal_matrix(perm, perm_size = NULL, basis = NULL)
```

print.gips	<i>Printing gips object</i>
------------	-----------------------------

Description

Printing function for a gips class.

Usage

```
## S3 method for class 'gips'
print(
  x,
  digits = 3,
  compare_to_original = TRUE,
  log_value = FALSE,
  oneline = FALSE,
  ...
)
```

Arguments

x	An object of a gips class.
digits	The number of digits after the comma for a posteriori to be presented. It can be negative. By default, Inf. It is passed to <code>base::round()</code> .
compare_to_original	A logical. Whether to print how many times more likely is the current permutation compared to: - the identity permutation () (for unoptimized gips object); - the starting permutation (for optimized gips object).
log_value	A logical. Whether to print the logarithmic value. Default to FALSE.
oneline	A logical. Whether to print in one or multiple lines. Default to FALSE.
...	The additional arguments passed to <code>base::cat()</code> .

Value

Returns an invisible NULL.

See Also

- `find_MAP()` - The function that makes an optimized gips object out of the unoptimized one.
- `compare_posteriories_of_perms()` - The function that prints the compared posteriories between any two permutations, not only compared to the starting one or id.

Examples

```
S <- matrix(c(1, 0.5, 0.5, 2), nrow = 2, byrow = TRUE)
g <- gips(S, 10, perm = "(12)")
print(g, digits = 4, oneline = TRUE)
```

print.gips_perm	<i>Printing gips_perm object</i>
-----------------	----------------------------------

Description

Printing function for a gips_perm class.

Usage

```
## S3 method for class 'gips_perm'
print(x, ...)
```

Arguments

x	An object of a gips_perm class.
...	Further arguments (currently ignored).

Value

Returns an invisible NULL.

Examples

```
gperm <- gips_perm("(5,4)", 5)
print(gperm)
```

project_matrix	<i>Project matrix after optimization</i>
----------------	--

Description

After the MAP permutation was found with `find_MAP()`, use this permutation to approximate the covariance matrix with bigger statistical confidence.

Usage

```
project_matrix(S, perm, precomputed_equal_indices = NULL)
```

Arguments

S	A square matrix to be projected. The empirical covariance matrix. (See the S parameter in the gips() function). When it is not positive semi-definite, it shows a warning of a class not_positive_semi_definite_matrix.
perm	A permutation to be projected on. An object of a gips class, a gips_perm class, or anything that can be used as the x argument in the gips_perm() function.
precomputed_equal_indices	This parameter is for internal use only.

Details

Project matrix on the space of symmetrical matrices invariant by a cyclic group generated by perm. This implements the formal [Definition 3 from references](#).

When S is the sample covariance matrix (output of cov() function, see examples), then S is the **unbiased estimator** of the covariance matrix. However, the **maximum likelihood estimator** of the covariance matrix is $S*(n-1)/(n)$, unless $n < p$, when the **maximum likelihood estimator does not exist**. For more information, see [Wikipedia - Estimation of covariance matrices](#).

The maximum likelihood estimator differs when one knows the covariance matrix is **invariant under some permutation**. This estimator will be symmetric AND have some values repeated (see examples and [Corollary 12 from references](#)).

The estimator will be invariant under the given permutation. Also, it will **need fewer observations** for the maximum likelihood estimator to exist (see [Project Matrix - Equation \(6\)](#) section in vignette("Theory", package = "gips") or in its [pkgdown page](#)). For some permutations, even $n = 2$ could be enough. The minimal number of observations needed are named n_0 and can be calculated by summary.gips().

For more details, see the [Project Matrix - Equation \(6\)](#) section in vignette("Theory", package = "gips") or in its [pkgdown page](#).

Value

Returns the matrix S projected on the space of symmetrical matrices invariant by a cyclic group generated by perm. See Details for more.

See Also

- [Wikipedia - Estimation of covariance matrices](#)
- [Project Matrix - Equation \(6\)](#) section of vignette("Theory", package = "gips") or its [pkgdown page](#) - A place to learn more about the math behind the gips package and see more examples of project_matrix().
- [find_MAP\(\)](#) - The function that finds the Maximum A Posteriori (MAP) Estimator for a given gips object. After the MAP Estimator is found, the matrix S can be projected on this permutation, creating the MAP Estimator of the covariance matrix (see examples).
- [gips_perm\(\)](#) - Constructor for the perm parameter.
- [plot.gips\(\)](#) - For plot(g, type = "MLE"), the project_matrix() is called (see examples).
- [summary.gips\(\)](#) - Can calculate the n_0 , the minimal number of observations, so that the projected matrix will be the MLE estimator of the covariance matrix.

Examples

```

p <- 6
my_perm <- "(14)(23)" # permutation (1,4)(2,3)(5)(6)
number_of_observations <- 10
X <- matrix(rnorm(p * number_of_observations), number_of_observations, p)
S <- cov(X)
projected_S <- project_matrix(S, perm = my_perm)
projected_S
# The value in [1,1] is the same as in [4,4]; also, [2,2] and [3,3];
# also [1,2] and [3,4]; also, [1,5] and [4,5]; and so on

# Plot the projected matrix:
g <- gips(S, number_of_observations, perm = my_perm)
plot(g, type = "MLE")

# Find the MAP Estimator of covariance
g_MAP <- find_MAP(g, max_iter = 10, show_progress_bar = FALSE, optimizer = "Metropolis_Hastings")
S_MAP <- project_matrix(attr(g, "S"), perm = g_MAP)
S_MAP
plot(g_MAP, type = "heatmap")

```

summary.gips

*Summarizing the gips object***Description**

summary method for gips class.

Usage

```

## S3 method for class 'gips'
summary(object, ...)

## S3 method for class 'summary.gips'
print(x, ...)

```

Arguments

object	An object of class gips. Usually, a result of a find_MAP() .
...	Further arguments passed to or from other methods.
x	An object of class summary.gips to be printed

Value

The function `summary.gips()` computes and returns a list of summary statistics of the given gips object. Those are:

- For unoptimized gips object:

1. `optimized` - FALSE.
 2. `start_permutation` - the permutation this gips represents.
 3. `start_permutation_log_posteriori` - the log of the a posteriori value the start permutation has.
 4. `times_more_likely_than_id` - how many more likely the `start_permutation` is over the identity permutation, `()`. It can be less than 1, meaning the identity permutation is more likely. Remember that this number can big and overflow to Inf or small and underflow to 0.
 5. `log_times_more_likely_than_id` - log of `times_more_likely_than_id`.
 6. `likelihood_ratio_test_statistics`, `likelihood_ratio_test_p_value` - statistics and p-value of Likelihood Ratio test, where the H_0 is that the data was drawn from the normal distribution with Covariance matrix invariant under the given permutation. The p-value is calculated from the asymptotic distribution. Note that this is sensibly defined only for $n \geq p$.
 7. `n0` - the minimum number of observations needed for the covariance matrix's maximum likelihood estimator (corresponding to a MAP) to exist. See *C σ and n0* section in `vignette("Theory", package = "gips")` or in its [pkgdown page](#).
 8. `S_matrix` - the underlying matrix. This matrix will be used in calculations of the posteriori value in `log_posteriori_of_gips()`.
 9. `number_of_observations` - the number of observations that were observed for the `S_matrix` to be calculated. This value will be used in calculations of the posteriori value in `log_posteriori_of_gips()`.
 10. `was_mean_estimated` - given by the user while creating the gips object:
 - TRUE means the S parameter was the output of `stats::cov()` function;
 - FALSE means the S parameter was calculated with `S = t(X) %*% X / number_of_observations`.
 11. `delta`, `D_matrix` - the hyperparameters of the Bayesian method. See the **Hyperparameters** section of `gips()` documentation.
 12. `n_parameters` - number of free parameters in the covariance matrix.
 13. AIC, BIC - output of `AIC.gips()` and `BIC.gips()` functions.
- For optimized gips object:
 1. `optimized` - TRUE.
 2. `found_permutation` - the permutation this gips represents. The visited permutation with the biggest a posteriori value.
 3. `found_permutation_log_posteriori` - the log of the a posteriori value the found permutation has.
 4. `start_permutation` - the original permutation this gips represented before optimization. It is the first visited permutation.
 5. `start_permutation_log_posteriori` - the log of the a posteriori value the start permutation has.
 6. `times_more_likely_than_start` - how many more likely the `found_permutation` is over the `start_permutation`. It cannot be a number less than 1. Remember that this number can big and overflow to Inf.
 7. `log_times_more_likely_than_start` - log of `times_more_likely_than_start`.
 8. `likelihood_ratio_test_statistics`, `likelihood_ratio_test_p_value` - statistics and p-value of Likelihood Ratio test, where the H_0 is that the data was drawn from the normal distribution with Covariance matrix invariant under `found_permutation`. The

p-value is calculated from the asymptotic distribution. Note that this is sensibly defined only for $n \geq p$.

9. `n0` - the minimal number of observations needed for the existence of the maximum likelihood estimator (corresponding to a MAP) of the covariance matrix (see `Cσ` and `n0` section in `vignette("Theory", package = "gips")` or in its [pkgdown page](#)).
10. `S_matrix` - the underlying matrix. This matrix will be used in calculations of the posteriori value in `log_posteriori_of_gips()`.
11. `number_of_observations` - the number of observations that were observed for the `S_matrix` to be calculated. This value will be used in calculations of the posteriori value in `log_posteriori_of_gips()`.
12. `was_mean_estimated` - given by the user while creating the `gips` object:
 - TRUE means the `S` parameter was output of the `stats::cov()` function;
 - FALSE means the `S` parameter was calculated with `S = t(X) %*% X / number_of_observations`.
13. `delta`, `D_matrix` - the hyperparameters of the Bayesian method. See the **Hyperparameters** section of `gips()` documentation.
14. `n_parameters` - number of free parameters in the covariance matrix.
15. `AIC`, `BIC` - output of `AIC.gips()` and `BIC.gips()` functions.
16. `optimization_algorithm_used` - all used optimization algorithms in order (one could start optimization with "MH", and then do an "HC").
17. `did_converge` - a boolean, did the last used algorithm converge.
18. `number_of_log_posteriori_calls` - how many times was the `log_posteriori_of_gips()` function called during the optimization.
19. `whole_optimization_time` - how long was the optimization process; the sum of all optimization times (when there were multiple).
20. `log_posteriori_calls_after_best` - how many times was the `log_posteriori_of_gips()` function called after the found permutation; in other words, how long ago could the optimization be stopped and have the same result. If this value is small, consider running `find_MAP()` again with `optimizer = "continue"`. For `optimizer = "BF"`, it is NULL.
21. `acceptance_rate` - only interesting for `optimizer = "MH"`. How often was the algorithm accepting the change of permutation in an iteration.

The function `print.summary.gips()` returns an invisible NULL.

Methods (by generic)

- `print(summary.gips)`: Printing method for class `summary.gips`. Prints every interesting information in a form pleasant for humans.

See Also

- `find_MAP()` - Usually, the `summary.gips()` is called on the output of `find_MAP()`.
- `log_posteriori_of_gips()` - Calculate the likelihood of a permutation.
- `AIC.gips()`, `BIC.gips()` - Calculate Akaike's or Bayesian Information Criterion
- `project_matrix()` - Project the known matrix on the found permutations space.

Examples

```

require("MASS") # for mvrnorm()

perm_size <- 6
mu <- runif(6, -10, 10) # Assume we don't know the mean
sigma_matrix <- matrix(
  data = c(
    1.1, 0.8, 0.6, 0.4, 0.6, 0.8,
    0.8, 1.1, 0.8, 0.6, 0.4, 0.6,
    0.6, 0.8, 1.1, 0.8, 0.6, 0.4,
    0.4, 0.6, 0.8, 1.1, 0.8, 0.6,
    0.6, 0.4, 0.6, 0.8, 1.1, 0.8,
    0.8, 0.6, 0.4, 0.6, 0.8, 1.1
  ),
  nrow = perm_size, byrow = TRUE
) # sigma_matrix is a matrix invariant under permutation (1,2,3,4,5,6)
number_of_observations <- 13
Z <- MASS::mvrnorm(number_of_observations, mu = mu, Sigma = sigma_matrix)
S <- cov(Z) # Assume we have to estimate the mean

g <- gips(S, number_of_observations)
unclass(summary(g))

g_map <- find_MAP(g, max_iter = 10, show_progress_bar = FALSE, optimizer = "Metropolis_Hastings")
unclass(summary(g_map))

g_map2 <- find_MAP(g, max_iter = 10, show_progress_bar = FALSE, optimizer = "hill_climbing")
summary(g_map2)
# =====
S <- matrix(c(1, 0.5, 0.5, 2), nrow = 2, byrow = TRUE)
g <- gips(S, 10)
print(summary(g))

```


Index

AIC(), 3
AIC.gips, 2
AIC.gips(), 10, 16, 20, 30, 31
as.character.gips, 4
as.character.gips(), 5, 16
as.character.gips_perm, 4
as.character.gips_perm(), 4, 5, 18

base::cat(), 26
base::round(), 26
BIC(), 3
BIC.gips(AIC.gips), 2
BIC.gips(), 10, 16, 20, 30, 31

calculate_gamma_function, 5
calculate_gamma_function(), 14, 21
compare_log_posteriories_of_perms
 (compare_posteriories_of_perms),
 6
compare_posteriories_of_perms, 6
compare_posteriories_of_perms(), 21, 26

find_MAP, 8
find_MAP(), 3, 7, 12–14, 16, 19–21, 23,
 26–29, 31
forget_perms, 11
forget_perms(), 10

get_probabilities_from_gips, 12
get_probabilities_from_gips(), 9, 10
get_structure_constants, 13
get_structure_constants(), 6, 21
gips, 14
gips(), 7, 10, 18, 23, 30, 31
gips_perm, 17
gips_perm(), 7, 16, 28

log_posteriori_of_gips, 20
log_posteriori_of_gips(), 6, 7, 10, 13, 14,
 23, 30, 31
logLik(), 20

logLik.gips, 19
logLik.gips(), 3, 16, 20

new_gips(gips), 14
new_gips_perm(gips_perm), 17

permutations::as.character.cycle(), 4,
 5
permutations::permutation(), 15, 17, 18
plot.gips, 22
plot.gips(), 10, 16, 28
prepare_orthogonal_matrix, 24
print.gips, 26
print.gips(), 7, 16
print.gips_perm, 27
print.gips_perm(), 18
print.summary.gips(summary.gips), 29
project_matrix, 27
project_matrix(), 3, 18–20, 23, 25, 31

stats::cov(), 15, 16, 30, 31
summary.gips, 29
summary.gips(), 7, 10, 16, 20, 28

validate_gips(gips), 14
validate_gips_perm(gips_perm), 17